

## 13.2 Find Probabilities Using Permutations

pp. 851–855

### EXAMPLE

You need to enter a 4 digit code in order to enter the building where you work. The digits are 4 different numbers from 1 to 5. You forgot the code and try to guess it. Find the probability that you guess correctly.

**STEP 1** Write the number of possible outcomes as the number of permutations of 4 out of the 5 possible digits. This is  ${}_5P_4$ .

$${}_5P_4 = \frac{5!}{(5-4)!} = \frac{5!}{1!} = 5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 120$$

**STEP 2** Find the probability. Because only one of the permutations is the correct code, the probability that you guess the correct code is  $\frac{1}{120}$ .

### EXERCISES

Evaluate the expression.

6.  ${}_7P_6$

7.  ${}_6P_2$

8.  ${}_8P_5$

9.  ${}_{13}P_{10}$

10. **MUSIC** You downloaded 6 songs. You randomly choose 4 of these songs to play. Find the probability that you play the first 4 songs you downloaded in the order in which you downloaded them.

### EXAMPLE 2

on p. 852  
for Exs. 6–10

## 13.3 Find Probabilities Using Combinations

pp. 856–859

### EXAMPLE

For your government class, you must choose 3 states in the United States to research. You may choose your states from the 6 New England states. How many combinations of states are possible?

The order in which you choose the states is not important. So, to find the number of combinations of 6 states taken 3 at a time, find  ${}_6C_3$ .

$$\begin{aligned} {}_6C_3 &= \frac{6!}{(6-3)! \cdot 3!} && \text{Combinations formula} \\ &= \frac{6 \cdot 5 \cdot 4 \cdot 3!}{3! \cdot (3 \cdot 2 \cdot 1)} && \text{Expand factorials.} \\ &= 20 && \text{Divide out common factor, 3!.} \\ &&& \text{Simplify.} \end{aligned}$$

### EXERCISES

Evaluate the expression.

11.  ${}_7C_6$

12.  ${}_6C_2$

13.  ${}_8C_5$

14.  ${}_{13}C_{10}$

15. **TICKETS** You win 5 tickets to a concert. In how many ways can you choose 4 friends out of a group of 9 to take with you to the concert?

### EXAMPLE 2

on p. 857  
for Exs. 11–15