

FINDING ZEROS Because a zero of a function is an x -intercept of the function's graph, you can use the function's graph to find the zeros of a function.

EXAMPLE 4 Find the zeros of a quadratic function

Find the zeros of $f(x) = x^2 + 6x - 7$.

ANOTHER WAY

You can find the zeros of a function by factoring:

$$\begin{aligned} f(x) &= x^2 + 6x - 7 \\ 0 &= x^2 + 6x - 7 \\ 0 &= (x + 7)(x - 1) \\ x &= -7 \text{ or } x = 1 \end{aligned}$$

Solution

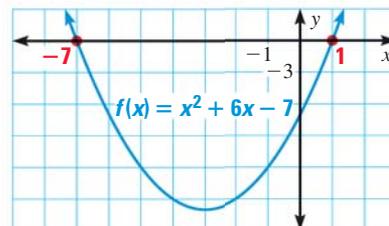
Graph the function $f(x) = x^2 + 6x - 7$.
The x -intercepts are -7 and 1 .

► The zeros of the function are -7 and 1 .

CHECK Substitute -7 and 1 in the original function.

$$f(-7) = (-7)^2 + 6(-7) - 7 = 0 \checkmark$$

$$f(1) = (1)^2 + 6(1) - 7 = 0 \checkmark$$



APPROXIMATING ZEROS The zeros of a function are not necessarily integers. To approximate zeros, look at the signs of the function values. If two function values have opposite signs, then a zero falls between the x -values that correspond to the function values.

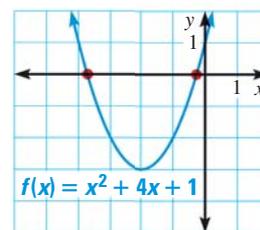
EXAMPLE 5 Approximate the zeros of a quadratic function

Approximate the zeros of $f(x) = x^2 + 4x + 1$ to the nearest tenth.

Solution

STEP 1 **Graph** the function $f(x) = x^2 + 4x + 1$. There are two x -intercepts: one between -4 and -3 and another between -1 and 0 .

STEP 2 **Make** a table of values for x -values between -4 and -3 and between -1 and 0 using an increment of 0.1 . Look for a change in the signs of the function values.



INTERPRET FUNCTION VALUES

The function value that is closest to 0 indicates the x -value that best approximates a zero of the function.

x	-3.9	-3.8	-3.7	-3.6	-3.5	-3.4	-3.3	-3.2	-3.1
$f(x)$	0.61	0.24	-0.11	-0.44	-0.75	-1.04	-1.31	-1.56	-1.79

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$f(x)$	-1.79	-1.56	-1.31	-1.04	-0.75	-0.44	-0.11	0.24	0.61

► In each table, the function value closest to 0 is -0.11 . So, the zeros of $f(x) = x^2 + 4x + 1$ are about -3.7 and about -0.3 .

GUIDED PRACTICE for Examples 4 and 5

- Find the zeros of $f(x) = x^2 + x - 6$.
- Approximate the zeros of $f(x) = -x^2 + 2x + 2$ to the nearest tenth.