

EXAMPLE 2 Use the substitution method

Solve the linear system: $x - 2y = -6$ Equation 1
 $4x + 6y = 4$ Equation 2

CHOOSE AN EQUATION

Equation 1 was chosen in Step 1 because x has a coefficient of 1. So, only one step is needed to solve Equation 1 for x .

Solution

STEP 1 Solve Equation 1 for x .

$$x - 2y = -6 \quad \text{Write original Equation 1.}$$

$$x = 2y - 6 \quad \text{Revised Equation 1}$$

STEP 2 Substitute $2y - 6$ for x in Equation 2 and solve for y .

$$4x + 6y = 4 \quad \text{Write Equation 2.}$$

$$4(2y - 6) + 6y = 4 \quad \text{Substitute } 2y - 6 \text{ for } x.$$

$$8y - 24 + 6y = 4 \quad \text{Distributive property}$$

$$14y - 24 = 4 \quad \text{Simplify.}$$

$$14y = 28 \quad \text{Add 24 to each side.}$$

$$y = 2 \quad \text{Divide each side by 14.}$$

STEP 3 Substitute 2 for y in the revised Equation 1 to find the value of x .

$$x = 2y - 6 \quad \text{Revised Equation 1}$$

$$x = 2(2) - 6 \quad \text{Substitute 2 for } y.$$

$$x = -2 \quad \text{Simplify.}$$

▶ The solution is $(-2, 2)$.

CHECK Substitute -2 for x and 2 for y in each of the original equations.

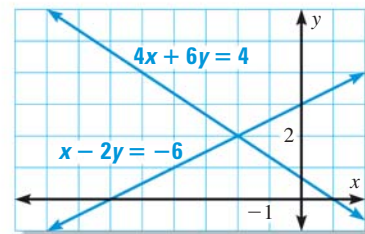
Equation 1

$$\begin{aligned} x - 2y &= -6 \\ -2 - 2(2) &\stackrel{?}{=} -6 \\ -6 &= -6 \quad \checkmark \end{aligned}$$

Equation 2

$$\begin{aligned} 4x + 6y &= 4 \\ 4(-2) + 6(2) &\stackrel{?}{=} 4 \\ 4 &= 4 \quad \checkmark \end{aligned}$$

CHECK REASONABLENESS When solving a linear system using the substitution method, you can use a graph to check the reasonableness of your solution. For example, the graph at the right verifies that $(-2, 2)$ is a solution of the linear system in Example 2.

**GUIDED PRACTICE** for Examples 1 and 2

Solve the linear system using the substitution method.

1. $y = 2x + 5$
 $3x + y = 10$

2. $x - y = 3$
 $x + 2y = -6$

3. $3x + y = -7$
 $-2x + 4y = 0$