PROPERTIES OF MULTIPLICATION Notice that both 4(-5) and -5(4) have a product of -20, so 4(-5) = -5(4). This equation is an example of the commutative property of multiplication. Properties of multiplication are listed below.

KEY CONCEPT

For Your Notebook

Properties of Multiplication

COMMUTATIVE PROPERTY The order in which you multiply two numbers does not change the product.

Algebra
$$a \cdot b = b \cdot a$$

Example
$$4 \cdot (-5) = -5 \cdot 4$$

ASSOCIATIVE PROPERTY The way you group three numbers in a product does not change the product.

Algebra
$$(a \cdot b) \cdot c = a \cdot (b \cdot c)$$

Example
$$(-2 \cdot 7) \cdot 4 = -2 \cdot (7 \cdot 4)$$

IDENTITY PROPERTY The product of a number and 1 is that number.

Algebra
$$a \cdot 1 = 1 \cdot a = a$$

Example
$$(-5) \cdot 1 = -5$$

PROPERTY OF ZERO The product of a number and 0 is 0.

Algebra
$$a \cdot 0 = 0 \cdot a = 0$$

Example
$$-3 \cdot 0 = 0$$

PROPERTY OF -1 The product of a number and -1 is the opposite of the number.

Algebra
$$a \cdot (-1) = -1 \cdot a = -a$$
 Example $-2 \cdot (-1) = 2$

Example
$$-2 \cdot (-1) = 1$$

The identity property states that the product of a number a and 1 is a. The number 1 is called the **multiplicative identity**.

EXAMPLE 2

Identify properties of multiplication

Statement

Property illustrated

a.
$$(x \cdot 7) \cdot 0.5 = x \cdot (7 \cdot 0.5)$$

b.
$$8 \cdot 0 = 0$$

c.
$$-6 \cdot y = y \cdot (-6)$$

d.
$$9 \cdot (-1) = -9$$

e. 1 •
$$v = v$$

Identity property of multiplication

GUIDED PRACTICE for Example 2

Identify the property illustrated.

4.
$$-1 \cdot 8 = -8$$

5.
$$12 \cdot x = x \cdot 12$$

6.
$$(y \cdot 4) \cdot 9 = y \cdot (4 \cdot 9)$$

7.
$$0 \cdot (-41) = 0$$

8.
$$-5 \cdot (-6) = -6 \cdot (-5)$$

9.
$$-13 \cdot (-1) = 13$$