Graph Quadratic Functions in Vertex Form 4.1.D, A.4.A; 2A.2.A, 2A.7.A

GOAL Graph quadratic functions in vertex form.

Key Vocabulary • vertex form

Extension

Use after Lesson 10.5

In Lesson 10.2, you graphed quadratic functions in standard form. Quadratic functions can also be written in **vertex form**, $y = a(x - h)^2 + k$ where $a \neq 0$. In this form, the vertex of the graph can be easily determined.

KEY CONCEPT

Graph of Vertex Form $y = a(x - h)^2 + k$

The graph of $y = a(x - h)^2 + k$ is the graph of $y = ax^2$ translated h units horizontally and k units vertically.

- Characteristics of the graph of $y = a(x h)^2 + k$:
- The vertex is (*h*, *k*).
- The axis of symmetry is x = h.
- The graph opens up if a > 0, and
- the graph opens down if a < 0.



For Your Notebook

EXAMPLE 1 Graph a quadratic function in vertex form

Graph $y = -(x + 2)^2 + 3$.

Solution

- **STEP 1** Identify the values of *a*, *h*, and *k*: a = -1, h = -2, and k = 3. Because a < 0, the parabola opens down.
- **STEP 2** Draw the axis of symmetry, x = -2.
- **STEP 3** Plot the vertex (h, k) = (-2, 3).
- *STEP 4* **Plot** four points. Evaluate the function for two *x*-values less than the *x*-coordinate of the vertex.
 - x = -3: $y = -(-3 + 2)^2 + 3 = 2$
 - x = -5: $y = -(-5 + 2)^2 + 3 = -6$

Plot the points (-3, 2) and (-5, -6) and their reflections, (-1, 2) and (1, -6), in the axis of symmetry.



STEP 5 **Draw** a parabola through the plotted points.