10.4

Use Square Roots to Solve Quadratic Equations



2A.6.B. 2A.8.D

You solved a quadratic equation by graphing.

Now

You will solve a quadratic equation by finding square roots.

Why?

So you can solve a problem about a falling object, as in Example 5.

Key Vocabulary

- square root, p. 110
- perfect square, p. 111

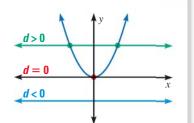
To use square roots to solve a quadratic equation of the form $ax^2 + c = 0$, first isolate x^2 on one side to obtain $x^2 = d$. Then use the following information about the solutions of $x^2 = d$ to solve the equation.

KEY CONCEPT

For Your Notebook

Solving $x^2 = d$ by Taking Square Roots

- If d > 0, then $x^2 = d$ has two solutions: $x = \pm \sqrt{d}$.
- If d = 0, then $x^2 = d$ has one solution: x = 0.
- If d < 0, then $x^2 = d$ has no solution.



READING

Recall that in this course, *solutions* refers to real-number solutions.

EXAMPLE 1

Solve quadratic equations

Solve the equation.

a.
$$2x^2 = 8$$

b.
$$m^2 - 18 = -18$$

c.
$$b^2 + 12 = 5$$

You can also use factoring to solve $2x^2 - 8 = 0$:

ANOTHER WAY

$$2x^{2} - 8 = 0.$$

$$2x^{2} - 8 = 0.$$

$$2(x^{2} - 4) = 0.$$

$$2(x - 2)(x + 2) = 0.$$

$$x = 2 \text{ or } x = -2$$

a.
$$2x^2 = 8$$

Solution

$$x^2 = 4$$

Divide each side by 2.

$$x = \pm \sqrt{4} = \pm 2$$

Take square roots of each side. Simplify.

 \blacktriangleright The solutions are -2 and 2.

b.
$$m^2 - 18 = -18$$

Write original equation.

$$m^2 = 0$$

Add 18 to each side.

$$m = 0$$

The square root of 0 is 0.

▶ The solution is 0.

c.
$$b^2 + 12 = 5$$

Write original equation.

$$b^2 = -7$$

Subtract 12 from each side.

Negative real numbers do not have real square roots. So, there is no solution.