Graph Quadratic Functions in Intercept Form 4.4.A; 2A.2.A, 2A.6.B

GOAL Graph quadratic functions in intercept form.

In Lesson 10.2 you graphed quadratic functions written in standard form. Quadratic functions can also be written in **intercept form**, y = a(x - p)(x - q) where $a \neq 0$. In this form, the *x*-intercepts of the graph can easily be determined.

KEY CONCEPT

Graph of Intercept Form y = a(x - p)(x - q)

Characteristics of the graph of y = a(x - p)(x - q):

- The *x*-intercepts are *p* and *q*.
- The axis of symmetry is halfway between (*p*, 0) and (*q*, 0). So, the axis of symmetry

is
$$x = \frac{p+q}{2}$$
.

• The parabola opens up if *a* > 0 and opens down if *a* < 0.

EXAMPLE 1 Graph a quadratic function in intercept form

Graph y = -(x + 1)(x - 5).

Solution

- **STEP 1** Identify and plot the *x*-intercepts. Because p = -1 and q = 5, the *x*-intercepts occur at the points (-1, 0) and (5, 0).
- *STEP 2* Find and draw the axis of symmetry.

$$x = \frac{p+q}{2} = \frac{-1+5}{2} = 2$$

STEP 3 Find and plot the vertex.

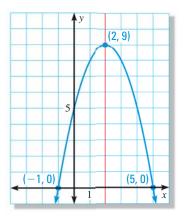
The *x*-coordinate of the vertex is 2.

To find the *y*-coordinate of the vertex, substitute **2** for *x* and simplify.

$$y = -(\mathbf{2} + 1)(\mathbf{2} - 5) = 9$$

So, the vertex is (2, 9).

STEP 4 **Draw** a parabola through the vertex and the points where the *x*-intercepts occur.



For Your Notebook

(p, 0)

 $x = \frac{p+q}{q}$

(q, 0)

FIND ZEROS OF A FUNCTION

Notice that the *x*-intercepts of the graph are also the zeros of the function: 0 = -(x + 1)(x - 5)x + 1 = 0 or x - 5 = 0x = -1 or x = 5

Extension

Use after Lesson 10.2

Key Vocabulary

• intercept form