FINDING A COMMON FACTOR In Lesson 9.4, you learned to factor out the greatest common monomial factor from the terms of a polynomial. Sometimes you may need to do this before finding two binomial factors of a trinomial.

## EXAMPLE 4 Write and solve a polynomial equation

DISCUS An athlete throws a discus from an initial height of 6 feet and with an initial vertical velocity of 46 feet per second.
a. Write an equation that gives the height (in feet) of the discus as a function of the time (in seconds) since it left the athlete's hand.
b. After how many seconds does the discus hit the ground?


## Solution

a. Use the vertical motion model to write an equation for the height $h$ (in feet) of the discus. In this case, $v=46$ and $s=6$.

$$
\begin{array}{ll}
h=-16 t^{2}+v t+s & \\
h=-16 t^{2}+46 t+6 & \\
\text { Vertical motion model } \\
h \text { Substitute } \mathbf{4 6} \text { for } \mathbf{v} \text { and } \mathbf{6} \text { for } \mathrm{s} .
\end{array}
$$

b. To find the number of seconds that pass before the discus lands, find the value of $t$ for which the height of the discus is 0 . Substitute 0 for $h$ and solve the equation for $t$.

$$
\begin{array}{ll}
\begin{array}{l}
0=-16 t^{2}+46 t+6
\end{array} & \text { Substitute } 0 \text { for } h . \\
0=-2\left(8 t^{2}-23 t-3\right) & \text { Factor out }-2 . \\
0=-2(8 t+1)(t-3) & \begin{array}{l}
\text { Factor the trinomial. Find factors of } 8 \text { and }-3 \text { that } \\
\text { produce a middle term with a coefficient of }-23 . \\
8 t+1=0 \quad \text { or } t-3=0
\end{array} \\
t=-\frac{1}{8} \text { or } \quad t=3 & \text { Sero-product property for } t .
\end{array}
$$

The solutions of the equation are $-\frac{1}{8}$ and 3 . A negative solution does not make sense in this situation, so disregard $-\frac{1}{8}$.

- The discus hits the ground after 3 seconds.


## GUIDED PRACTICE for Example 4

7. WHAT IF? In Example 4, suppose another athlete throws the discus with an initial vertical velocity of 38 feet per second and releases it from a height of 5 feet. After how many seconds does the discus hit the ground?
8. SHOT PUT In a shot put event, an athlete throws the shot put from an initial height of 6 feet and with an initial vertical velocity of 29 feet per second. After how many seconds does the shot put hit the ground?
