FACTORING When factoring a trinomial, first consider the signs of $p$ and $q$.

| $(x+p)(x+q)$ | $x^{2}+b x+c$ | Signs of $b$ and $c$ |
| :--- | :--- | :--- |
| $(x+2)(x+3)$ | $x^{2}+5 x+6$ | $b$ is positive; $c$ is positive. |
| $(x+2)(x+(-3))$ | $x^{2}-x-6$ | $b$ is negative; $c$ is negative. |
| $(x+(-2))(x+3)$ | $x^{2}+x-6$ | $b$ is positive; $c$ is negative. |
| $(x+(-2))(x+(-3))$ | $x^{2}-5 x+6$ | $b$ is negative; $c$ is positive. |

By observing the signs of $b$ and $c$ in the table, you can see that:

- $b$ and $c$ are positive when both $p$ and $q$ are positive.
- $b$ is negative and $c$ is positive when both $p$ and $q$ are negative.
- $c$ is negative when $p$ and $q$ have different signs.


## EXAMPLE 2 Factor when $\boldsymbol{b}$ is negative and $\boldsymbol{c}$ is positive

Factor $\boldsymbol{n}^{2}-\mathbf{6 n}+8$.
Because $b$ is negative and $c$ is positive, $p$ and $q$ must both be negative.

| Factors of 8 | Sum of factors |  |
| :---: | :---: | :---: |
| -8, -1 | $-8+(-1)=-9$ | $x$ |
| -4, -2 | $-4+(-2)=-6$ | $\longleftarrow$ Correct sum |

## EXAMPLE 3 Factor when $b$ is positive and $c$ is negative

Factor $\boldsymbol{y}^{2}+2 y-15$.
Because $c$ is negative, $p$ and $q$ must have different signs.

| Factors of -15 | Sum of factors | $x$ |
| :---: | :---: | :---: |
| -15, 1 | $-15+1=-14$ |  |
| 15, -1 | $15+(-1)=14$ | $x$ |
| $-5,3$ | $-5+3=-2$ | $x$ |
| 5, -3 | $5+(-3)=2$ |  |

$y^{2}+2 y-15=(y+5)(y-3)$

## GUIDED PRACTICE for Examples 2 and 3

## Factor the trinomial.

4. $x^{2}-4 x+3$
5. $t^{2}-8 t+12$
6. $m^{2}+m-20$
7. $w^{2}+6 w-16$
