

FUNCTIONS The table shows that a rule for finding the n th term of a geometric sequence is $a_n = a_1 r^{n-1}$. Notice that the rule is an exponential function.

		+ 1	+ 1	+ 1	+ 1	
Position, n	1	2	3	4	...	n
Term, a_n	a_1	$a_1 r$	$a_1 r^2$	$a_1 r^3$...	$a_1 r^{n-1}$

• r • r • r • r

For the n th term, you multiply a_1 by $r(n - 1)$ times.

KEY CONCEPT
For Your Notebook

General Rule for a Geometric Sequence

The n th term of a geometric sequence with first term a_1 and common ratio r is given by: $a_n = a_1 r^{n-1}$.

EXAMPLE 3
Write a rule for a geometric sequence

Write a rule for the n th term of the geometric sequence in Example 1. Then find a_{10} .

Solution

To write a rule for the n th term of the sequence, substitute the values for a_1 and r in the general rule $a_n = a_1 r^{n-1}$. Because $a_1 = 128$ and $r = \frac{1}{2}$, $a_n = 128 \cdot \left(\frac{1}{2}\right)^{n-1}$. The 10th term of the sequence is $a_{10} = 128 \cdot \left(\frac{1}{2}\right)^{10-1} = \frac{1}{4}$.

PRACTICE

EXAMPLES 1, 2, and 3
on pp. 539–540
for Exs. 1–10

- Tell whether the sequence is *arithmetic* or *geometric*. Then graph the sequence.
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|--------------------------|-------------------------|------------------------|
| 1. 3, 12, 48, 192, ... | 2. 7, 16, 25, 34, ... | 3. 34, 28, 22, 16, ... |
| 4. 1024, 128, 16, 2, ... | 5. 9, -18, 36, -72, ... | 6. 29, 43, 57, 71, ... |

- Write a rule for the n th term of the geometric sequence. Then find a_7 .**
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| 7. 1, -5, 25, -125, ... | 8. 13, 26, 52, 104, ... | 9. 432, 72, 12, 2, ... |
|-------------------------|-------------------------|------------------------|

10. E-MAIL A chain e-mail instructs the recipient to forward the e-mail to four more people. The table shows the number of rounds of sending the e-mail and the number of new e-mails generated. Write a rule for the n th term of the sequence. Then graph the first six terms of the sequence.

Number of rounds sending e-mail, n	1	2	3	4
Number of new e-mails generated, a_n	1	4	16	64