

ANOTHER WAY In Example 3, you could solve $2 < x + 5 < 9$ by subtracting 5 from 2, $x + 5$, and 9 without first separating the compound inequality into two separate inequalities. To solve a compound inequality with *and*, you perform the same operation on each expression.

EXAMPLE 4 Solve a compound inequality with *and*

Solve $-5 \leq -x - 3 \leq 2$. Graph your solution.

$$-5 \leq -x - 3 \leq 2$$

Write original inequality.

$$-5 + 3 \leq -x - 3 + 3 \leq 2 + 3$$

Add 3 to each expression.

$$-2 \leq -x \leq 5$$

Simplify.

$$-1(-2) \geq -1(-x) \geq -1(5)$$

Multiply each expression by -1 and reverse *both* inequality symbols.

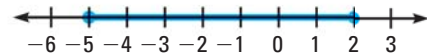
$$2 \geq x \geq -5$$

Simplify.

$$-5 \leq x \leq 2$$

Rewrite in the form $a \leq x \leq b$.

► The solutions are all real numbers greater than or equal to -5 and less than or equal to 2 .



EXAMPLE 5 Solve a compound inequality with *or*

Solve $2x + 3 < 9$ or $3x - 6 > 12$. Graph your solution.

Solution

Solve the two inequalities separately.

$$2x + 3 < 9$$

or

$$3x - 6 > 12$$

Write original inequality.

$$2x + 3 - 3 < 9 - 3$$

or

$$3x - 6 + 6 > 12 + 6$$

Addition or subtraction property of inequality

$$2x < 6$$

or

$$3x > 18$$

Simplify.

$$\frac{2x}{2} < \frac{6}{2}$$

or

$$\frac{3x}{3} > \frac{18}{3}$$

Division property of inequality

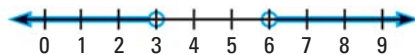
$$x < 3$$

or

$$x > 6$$

Simplify.

► The solutions are all real numbers less than 3 or greater than 6.



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GUIDED PRACTICE for Examples 4 and 5

Solve the inequality. Graph your solution.

7. $-14 < x - 8 < -1$

8. $-1 \leq -5t + 2 \leq 4$

9. $3h + 1 < -5$ or $2h - 5 > 7$

10. $4c + 1 \leq -3$ or $5c - 3 > 17$