## EXAMPLE 2 Write an equation given two points

Write an equation of the line that passes through $(-2,5)$ and $(2,-1)$.

## Solution

STEP 1 Calculate the slope.

$$
m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{-1-5}{2-(-2)}=\frac{-6}{4}=-\frac{3}{2}
$$

## ANOTHER WAY

You can also find the $y$-intercept using the coordinates of the other given point, $(2,-1)$ :
$y=m x+b$
$-1=-\frac{3}{2}(2)+b$
$2=b$

STEP 2 Find the $y$-intercept. Use the slope and the point $(-2,5)$.

$$
\begin{array}{ll}
y=m x+b & \text { Write slope-intercept form. } \\
5=-\frac{3}{2}(-2)+b & \text { Substitute }-\frac{3}{2} \text { for } m,-2 \text { for } x, \text { and } 5 \text { for } y . \\
2=b & \text { Solve for } b .
\end{array}
$$

STEP 3 Write an equation of the line.

$$
\begin{array}{ll}
y=m x+b & \text { Write slope-intercept form. } \\
y=-\frac{3}{2} x+2 & \text { Substitute }-\frac{3}{2} \text { for } m \text { and } 2 \text { for } b .
\end{array}
$$

## ELIMINATE CHOICES

You can also evaluate each function when $x=2$ and $x=-2$. Eliminate any choices for which $f(2) \neq 4$ or $f(-2) \neq-8$.

## Example 3 TAKS PRACTICE: Multiple Choice

Which function has the values $f(2)=4$ and $f(-2)=-8$ ?
(A) $f(x)=3 x-10$
(B) $f(x)=3 x-2$
(C) $f(x)=3 x+2$
(D) $f(x)=3 x+20$

STEP 1 Calculate the slope. Write $f(2)=4$ as $(2,4)$ and $f(-2)=-8$ as $(-2,-8)$.

$$
m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{-8-4}{-2-2}=\frac{-12}{-4}=\mathbf{3}
$$

STEP 2 Find the $y$-intercept. Use the slope and the point $(2,4)$.

$$
\begin{aligned}
y & =m x+b & & \text { Write slope-intercept form. } \\
4 & =3(2)+b & & \text { Substitute } \mathbf{3} \text { for } \boldsymbol{m}, 2 \text { for } \boldsymbol{x}, \text { and } 4 \text { for } y . \\
-2 & =b & & \text { Solve for } b .
\end{aligned}
$$

STEP 3 Write an equation for the function. Use function notation.

$$
f(x)=3 x-2 \quad \text { Substitute } 3 \text { for } m \text { and }-2 \text { for } b .
$$

The answer is B. (A) (B) (C) (D)

## Guided Practice for Examples 2 and 3

2. Write an equation of the line that passes through $(1,-2)$ and $(-5,4)$.
3. Write an equation for the linear function with the values $f(-2)=10$ and $f(4)=-2$.
