USING TWO POINTS If you know the point where a line crosses the $y$-axis and any other point on the line, you can write an equation of the line.

## EXAMPLE 3 Write an equation of a line given two points

Write an equation of the line shown.

## Solution

STEP 1 Calculate the slope.

$$
m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{-1-(-5)}{3-0}=\frac{4}{3}
$$

STEP 2 Write an equation of the line. The line crosses the $y$-axis at $(0,-5)$. So, the $y$-intercept is -5 .

$y=m x+b \quad$ Write slope-intercept form.
$y=\frac{4}{3} x-5 \quad$ Substitute $\frac{4}{3}$ for $m$ and -5 for $b$.

WRIITING FUNCTIONS Recall that the graphs of linear functions are lines. You can use slope-intercept form to write a linear function.

## EXAMPLE 4 Write a linear function

FUNCTIONS For help with using function notation, see p. 262.

Write an equation for the linear function $f$ with the values $f(0)=5$ and $f(4)=17$.

## Solution

STEP 1 Write $f(0)=5$ as $(0,5)$ and $f(4)=17$ as $(4,17)$.
STEP 2 Calculate the slope of the line that passes through $(0,5)$ and $(4,17)$.
$m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{17-5}{4-0}=\frac{12}{4}=3$
STEP 3 Write an equation of the line. The line crosses the $y$-axis at $(0,5)$. So, the $y$-intercept is 5 .
$y=m x+b \quad$ Write slope-intercept form.
$y=3 x+5 \quad$ Substitute 3 for $m$ and 5 for $b$.
The function is $f(x)=3 x+5$.

## GUIDED PRACTICE for Examples 3 and 4

3. Write an equation of the line shown.

Write an equation for the linear function $f$ with the given values.
4. $f(0)=-2, f(8)=4$
5. $f(-3)=6, f(0)=5$


