43. MULTI-STEP PROBLEM A photographer is at a height $h$ taking aerial photographs. The ratio of the image length $W Q$ to the length $N A$ of the actual object is

$$
\frac{W Q}{N A}=\frac{f \tan (\theta-t)+f \tan t}{h \tan \theta}
$$

where $f$ is the focal length of the camera, $\theta$ is the angle between the vertical line perpendicular to the ground and the line from the camera to point $A$, and $t$ is the tilt angle of the film.
a. Use the difference formula for tangent to simplify the ratio.

b. Show that $\frac{W Q}{N A}=\frac{f}{h}$ when $t=0$.
44. TAKS REASONING Your friend pulls on a weight attached to a spring and then releases it. A split second later, you begin filming the spring to analyze its motion. You find that the spring's distance $y$ (in inches) from its equilibrium point can be modeled by $y=5 \sin (2 t+C)$ where $C=\tan ^{-1} \frac{3}{4}$ and $t$ is the elapsed time (in seconds) since you began filming.
a. Find the values of $\sin C$ and $\cos C$.
b. Use a sum formula to show that $y=5 \sin (2 t+C)$ can be written as $y=4 \sin 2 t+3 \cos 2 t$.
c. Graph the function found in part (b) and find its maximum value. Explain what this value represents.

45. CHALLENGE The busy signal on a touch-tone phone is a combination of two tones with frequencies of 480 hertz and 620 hertz. The individual tones can be modeled by the following equations:

```
480 hertz: }\mp@subsup{y}{1}{}=\operatorname{cos}960\pit\quad620\mathrm{ hertz: }\mp@subsup{y}{2}{}=\operatorname{cos}1240\pi
```

The sound of the busy signal can be modeled by $y_{1}+y_{2}$. Show that:

$$
y_{1}+y_{2}=2 \cos 1100 \pi t \cos 140 \pi t
$$

## MIXED REVIEW FOR TAKS

## TAKS PRACTICE at classzone.com

REVIEW
Lesson 12.1;
TAKS Workbook

## REVIEW

TAKS Workbook
46. TAKS PRACTICE A stack of boxes forms a square pyramid. The diagram shows the top three layers of the pyramid. Which rule gives the number $a_{n}$ of boxes in the $n$th layer of the pyramid? TAKS Obj. 2

(A) $a_{n}=2 n$
(B) $a_{n}=2(n+1)$
(C) $a_{n}=n(n+1)$
(D) $a_{n}=n^{2}$
47. TAKS PRACTICE What is the solution of $2(x-2)-1.45=3(x-3)$ ? TAKS Obj. 4
(F) -12.14
(G) 3.55
(H) 6.08
(J) 11.25

