SOLVING TRIGONOMETRIC EQUATIONS Solve the equation for $0 \le x < 2\pi$.

33.
$$\cos\left(x + \frac{\pi}{6}\right) - 1 = \cos\left(x - \frac{\pi}{6}\right)$$

35.
$$\sin\left(x + \frac{5\pi}{6}\right) + \sin\left(x - \frac{5\pi}{6}\right) = 1$$

37.
$$\tan(x + \pi) + 2\sin(x + \pi) = 0$$

- **39. CHALLENGE** Consider a complex number z = a + bi in the complex plane shown. Let *r* be the length of the line segment joining *z* and the origin, and let θ be the angle that this segment makes with the positive real axis, as shown.
 - **a.** *Explain* why $a = r \cos \theta$ and $b = r \sin \theta$, so that $z = (r \cos \theta) + i(r \sin \theta)$.
 - **b.** Use the result from part (a) to show the following:

$$z^{2} = r^{2}[(\cos\theta\cos\theta - \sin\theta\sin\theta) + i(\sin\theta\cos\theta + \cos\theta\sin\theta)]$$

c. Use the sum and difference formulas to show that the equation in part (b) can be written as $z^2 = r^2(\cos 2\theta + i \sin 2\theta)$.

PROBLEM SOLVING

EXAMPLE 5 on p. 951 for Exs. 40-41 **40. METEOROLOGY** The number *h* of hours of daylight for Rome, Italy, and Miami, Florida, can be approximated by the equations below, where *t* is the time in days and t = 0 represents January 1.

Rome:
$$h_1 = 2.7 \sin\left(\frac{\pi t}{182} - 4.94\right) + 12.1$$
 Miami: $h_2 = -1.6 \cos\frac{\pi t}{182} + 12.1$

On which days of the year will the cities have the same amount of daylight?

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41. CLOCK TOWER The heights *m* and *h* (in feet) of a clock tower's minute hand and hour hand, respectively, can be approximated by

$$m = 182.5 - 11.5 \sin\left(\frac{\pi t}{30} - \frac{\pi}{2}\right)$$
 and $h = 182.5 - 7 \sin\left(\frac{\pi t}{360}\right)$

where *t* is the time in minutes and t = 0 represents 3:00 P.M. Use a graphing calculator to find how long it takes for the height of the minute hand to equal the height of the hour hand.

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42. PHYSICAL SCIENCE When a wave travels through a taut string, the displacement *y* of each point on the string depends on the time *t* and the point's position *x*. The equation of a *standing wave* can be obtained by adding the displacements of two waves traveling in opposite directions. Suppose two waves can be modeled by these equations:

$$y_1 = A\cos\left(\frac{2\pi t}{3} - \frac{2\pi x}{5}\right) \qquad \qquad y_2 = A\cos\left(\frac{2\pi t}{3} + \frac{2\pi x}{5}\right)$$

Show that $y_1 + y_2 = 2A\cos\left(\frac{2\pi t}{3}\right)\cos\left(\frac{2\pi x}{5}\right)$.





34. $\sin\left(x + \frac{\pi}{4}\right) + \sin\left(x - \frac{\pi}{4}\right) = 0$

36. $\tan(x + \pi) + \cos\left(x + \frac{\pi}{2}\right) = 0$

38. $\sin(x + \pi) + \cos(x + \pi) = 0$