

13.4 EXERCISES

HOMEWORK KEY

 = **WORKED-OUT SOLUTIONS**
on p. WS1 for Exs. 7, 23, and 37

 = **TAKS PRACTICE AND REASONING**
Exs. 11, 30, 31, 37, 38, 41, and 42

SKILL PRACTICE

1. **VOCABULARY** Copy and complete: The ? sine of $\frac{1}{2}$ is $\frac{\pi}{6}$, or 30° .

2. **WRITING** Explain why $\tan^{-1} 3$ is defined, but $\cos^{-1} 3$ is undefined.

EXAMPLE 1

on p. 876
for Exs. 3–11

EVALUATING EXPRESSIONS Evaluate the expression without using a calculator. Give your answer in both radians and degrees.

3. $\sin^{-1} 1$

4. $\tan^{-1} (-1)$

5. $\cos^{-1} 0$

6. $\cos^{-1} (-2)$

7. $\sin^{-1} \frac{\sqrt{3}}{2}$

8. $\sin^{-1} \frac{1}{2}$

9. $\tan^{-1} \left(-\frac{\sqrt{3}}{3} \right)$

10. $\cos^{-1} \left(-\frac{1}{2} \right)$

11.  **TAKS REASONING** What is the value of the expression $\cos^{-1} \frac{\sqrt{2}}{2}$?

(A) 0°

(B) 30°

(C) 45°

(D) 60°

USING A CALCULATOR Use a calculator to evaluate the expression in both radians and degrees.

12. $\sin^{-1} 0.18$

13. $\tan^{-1} 2.6$

14. $\cos^{-1} 0.36$

15. $\cos^{-1} (-0.4)$

16. $\tan^{-1} (-0.75)$

17. $\sin^{-1} (-0.2)$

18. $\sin^{-1} 0.8$

19. $\cos^{-1} 0.99$

EXAMPLE 2

on p. 876
for Exs. 20–26

SOLVING EQUATIONS Solve the equation for θ .

20. $\cos \theta = -0.82$; $180^\circ < \theta < 270^\circ$

21. $\sin \theta = -0.45$; $180^\circ < \theta < 270^\circ$

22. $\sin \theta = 0.15$; $90^\circ < \theta < 180^\circ$

23. $\tan \theta = 3.2$; $180^\circ < \theta < 270^\circ$

24. $\tan \theta = -5.3$; $90^\circ < \theta < 180^\circ$

25. $\cos \theta = 0.25$; $270^\circ < \theta < 360^\circ$

26. **ERROR ANALYSIS** Describe and correct the error in solving the equation $\sin \theta = 0.7$ where $90^\circ < \theta < 180^\circ$.

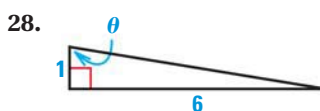
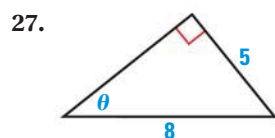
The angle whose sine is 0.7 is $\sin^{-1} 0.7 \approx 44.4^\circ$, so $\theta \approx 44.4^\circ$.





EXAMPLE 3

on p. 877
for Exs. 27–29

FINDING ANGLES Find the measure of the angle θ .



30.  **TAKS REASONING** Suppose $\cos \theta > 0$ and $\sin \theta < 0$. Give a possible value of θ such that $-360^\circ \leq \theta \leq 0^\circ$.

31.  **TAKS REASONING** Suppose $\sin \theta < 0$ and $\tan \theta > 0$. Give a possible value of θ such that $360^\circ \leq \theta \leq 720^\circ$.

CHALLENGE Rewrite the expression so that it does not involve trigonometric functions or inverse trigonometric functions.

32. $\csc (\sin^{-1} x)$

33. $\cot (\tan^{-1} x)$

34. $\sec (\cos^{-1} x)$