23. **TAKS REASONING** Create a data set with a mean of 10, a median of 11, and a mode of 8.

24. 👆 TAKS REASONING An outlier can be defined as a value in a data set that lies more than three standard deviations from the mean. So, x is an outlier if $\frac{|x - \overline{x}|}{|x - \overline{x}||} > 3$. In parts (a)–(c), use this definition to identify the outlier(s)

in the data set. Justify your answers mathematically.

- a. 70, 55, 54, 75, 60, 58, 55, 56, 6, 62, 68, 94, 55, 82, 69, 74
- **b.** 18, 20, 22, 25, 16, 40, 24, 19, 38, 3, 21, 27, 88, 24, 23, 26
- c. 50, 93, 81, 84, 88, 85, 90, 99, 92, 199, 96, 89, 87, 94, 37

25. CHALLENGE The formula for standard deviation can also be written as:

$$\sigma = \sqrt{\frac{x_1^2 + x_2^2 + \dots + x_n^2}{n} - \overline{x}^2}$$

For n = 3, show that this formula is equivalent to the formula given on page 745. (*Hint:* You will need to show that $x_1 + x_2 + x_3 = 3\overline{x}$.)

PROBLEM SOLVING

