EXAMPLE 2) TAKS PRACTICE: Multiple Choice

A card is randomly selected from a standard deck of 52 cards. What is the probability that it is a heart *or* a three?

(A)
$$\frac{4}{13}$$
 (B) $\frac{17}{52}$ (C) $\frac{25}{52}$ (D) $\frac{7}{13}$

Solution

Let event *A* be selecting a heart and event *B* be selecting a three. *A* has 13 outcomes and *B* has 4 outcomes. Of these, 1 outcome is common to *A* and *B*. So, the probability of selecting a heart *or* a three is:



$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) = \frac{13}{52} + \frac{4}{52} - \frac{1}{52} = \frac{16}{52} = \frac{4}{13}$$

The correct answer is A. (A) (B) \bigcirc (D)

EXAMPLE 3 Use a formula to find *P*(*A* and *B*)

SENIOR CLASS Out of 200 students in a senior class, 113 students are either varsity athletes *or* on the honor roll. There are 74 seniors who are varsity athletes and 51 seniors who are on the honor roll. What is the probability that a randomly selected senior is both a varsity athlete *and* on the honor roll?

Solution

Let event *A* be selecting a senior who is a varsity athlete and event *B* be selecting a senior on the honor roll. From the given information you know that

$$P(A) = \frac{74}{200}, P(B) = \frac{51}{200}, \text{ and } P(A \text{ or } B) = \frac{113}{200}. \text{ Find } P(A \text{ and } B).$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) \quad \text{Write general formula.}$$

$$\frac{113}{200} = \frac{74}{200} + \frac{51}{200} - P(A \text{ and } B) \quad \text{Substitute known probabilities.}$$

$$P(A \text{ and } B) = \frac{74}{200} + \frac{51}{200} - \frac{113}{200} \quad \text{Solve for } P(A \text{ and } B).$$

$$P(A \text{ and } B) = \frac{12}{200} = \frac{3}{50} = 0.06 \quad \text{Simplify.}$$

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GUIDED PRACTICE for Examples 1, 2, and 3

A card is randomly selected from a standard deck of 52 cards. Find the probability of the given event.

- 1. Selecting an ace or an eight2. Selecting a 10 or a diamond
- **3. WHAT IF?** In Example 3, suppose 32 seniors are in the band and 64 seniors are in the band *or* on the honor roll. What is the probability that a randomly selected senior is both in the band *and* on the honor roll?