

**MULTIPLE EVENTS** When finding the number of ways both an event  $A$  and an event  $B$  can occur, you need to multiply, as in part (b) of Example 1. When finding the number of ways that event  $A$  or event  $B$  can occur, you add instead.

### EXAMPLE 2 Decide to multiply or add combinations

**THEATER** William Shakespeare wrote 38 plays that can be divided into three genres. Of the 38 plays, 18 are comedies, 10 are histories, and 10 are tragedies.

- How many different sets of *exactly* 2 comedies and 1 tragedy can you read?
- How many different sets of *at most* 3 plays can you read?

#### Solution

- You can choose **2** of the **18** comedies and **1** of the **10** tragedies. So, the number of possible sets of plays is:

$${}_{18}C_2 \cdot {}_{10}C_1 = \frac{18!}{16! \cdot 2!} \cdot \frac{10!}{9! \cdot 1!} = \frac{18 \cdot 17 \cdot \cancel{16!}}{\cancel{16!} \cdot 2 \cdot 1} \cdot \frac{10 \cdot \cancel{9!}}{\cancel{9!} \cdot 1} = 153 \cdot 10 = 1530$$

- You can read **0**, **1**, **2**, or **3** plays. Because there are **38** plays that can be chosen, the number of possible sets of plays is:

$${}_{38}C_0 + {}_{38}C_1 + {}_{38}C_2 + {}_{38}C_3 = 1 + 38 + 703 + 8436 = 9178$$

#### AVOID ERRORS

When finding the number of ways to select *at most*  $n$  objects, be sure to include the possibility of selecting 0 objects.

**SUBTRACTING POSSIBILITIES** Counting problems that involve phrases like “at least” or “at most” are sometimes easier to solve by subtracting possibilities you do not want from the total number of possibilities.



### EXAMPLE 3 TAKS REASONING: Multi-Step Problem

**BASKETBALL** During the school year, the girl’s basketball team is scheduled to play 12 home games. You want to attend *at least* 3 of the games. How many different combinations of games can you attend?

#### Solution

Of the **12** home games, you want to attend **3** games, or **4** games, or **5** games, and so on. So, the number of combinations of games you can attend is:

$${}_{12}C_3 + {}_{12}C_4 + {}_{12}C_5 + \cdots + {}_{12}C_{12}$$

Instead of adding these combinations, use the following reasoning. For each of the **12** games, you can choose to attend or not attend the game, so there are  $2^{12}$  total combinations. If you attend at least 3 games, you do not attend only a total of **0**, **1**, or **2** games. So, the number of ways you can attend at least 3 games is:

$$2^{12} - ({}_{12}C_0 + {}_{12}C_1 + {}_{12}C_2) = 4096 - (1 + 12 + 66) = 4017$$



#### GUIDED PRACTICE for Examples 1, 2, and 3

Find the number of combinations.

1.  ${}_8C_3$

2.  ${}_{10}C_6$

3.  ${}_7C_2$

4.  ${}_{14}C_5$

5. **WHAT IF?** In Example 2, how many different sets of *exactly* 3 tragedies and 2 histories can you read?