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CHAPTER TEST

Find the distance between the two points. Then find the midpoint of the line segment joining the two points.

1. $(-1, 5), (7, 3)$

2. $(4, 2), (8, 8)$

3. $(-1, -6), (1, 5)$

4. $(2, -5), (3, 1)$

5. $(-6, -2), (-3, 5)$

6. $(1, 9), (10, -2)$

Graph the equation.

7. $y^2 - 24x = 0$

8. $x^2 + y^2 = 16$

9. $64y^2 - x^2 = 64$

10. $18x^2 + 2y^2 = 18$

11. $(x - 6)^2 + (y + 1)^2 = 36$

12. $(x + 4)^2 = 6(y - 2)$

13. $\frac{(x + 4)^2}{9} - \frac{(y - 7)^2}{49} = 1$

14. $\frac{(x - 8)^2}{81} + \frac{(y - 2)^2}{100} = 1$

15. $\frac{(y - 5)^2}{9} - (x + 3)^2 = 1$

Write the standard form of the equation of the conic section with the given characteristics.

16. Parabola with vertex at $(0, 0)$ and directrix at $x = -6$ 17. Parabola with vertex at $(-2, -1)$ and focus at $(-2, 5)$ 18. Circle with center at $(0, 0)$ and passing through $(-5, 2)$ 19. Circle with center at $(1, -4)$ and radius 620. Ellipse with center at $(0, 0)$, vertex at $(0, 6)$, and co-vertex at $(-3, 0)$ 21. Ellipse with vertices at $(-1, 4)$ and $(7, 4)$ and foci at $(1, 4)$ and $(5, 4)$ 22. Hyperbola with vertices at $(0, -6)$ and $(0, 6)$ and foci at $(0, -9)$ and $(0, 9)$ 23. Hyperbola with vertex at $(2, -5)$, focus at $(-1, -5)$, and center at $(5, -5)$

Classify the conic section and write its equation in standard form.

24. $x^2 + 4y^2 - 6x - 16y + 21 = 0$

25. $x^2 + y^2 + 8x + 12y + 3 = 0$

26. $4x^2 - 9y^2 - 40x + 64 = 0$

27. $y^2 - 16y - 12x + 40 = 0$

28. $25x^2 + 4y^2 + 50x - 24y - 39 = 0$

29. $y^2 - 16x^2 + 14y + 64x - 31 = 0$

Solve the system.

30. $4x^2 + y^2 = 16$
 $x + y = 2$

31. $x^2 + 4y^2 - 8y = 4$
 $y^2 - 2y - 8x - 16 = 0$

32. $y^2 - x^2 + 2x - 5 = 0$
 $x^2 + y^2 - 2x - 3 = 0$

33. **WATER SURFACE** A cylindrical glass of water has a 1.5 inch radius. If the glass is tilted 60° , the water's surface meets the glass in an ellipse with minor axis 3 inches long and major axis 6 inches long. Write equations that model the water's surface with the glass upright and after the glass is tilted. Use the center of the water's surface as the origin.

34. **ASTRONOMY** The Green Bank Telescope in West Virginia has a main reflector whose cross section is a portion of a "parent" parabola. A diagram of the reflector's cross section and the parent parabola is shown. Write an equation that models the parent parabola if its vertex is at $(0, 0)$. What is the distance from the vertex to the focus?

