EXAMPLE 4 Subtract with unlike denominators

Subtract:
$$\frac{x+2}{2x-2} - \frac{-2x-1}{x^2-4x+3}$$

Solution

$$\frac{x+2}{2x-2} - \frac{-2x-1}{x^2-4x+3}$$

$$= \frac{x+2}{2(x-1)} - \frac{-2x-1}{(x-1)(x-3)}$$
Factor denominators.
$$= \frac{x+2}{2(x-1)} \cdot \frac{x-3}{x-3} - \frac{-2x-1}{(x-1)(x-3)} \cdot \frac{2}{2}$$
LCD is $2(x-1)(x-3)$.
$$= \frac{x^2-x-6}{2(x-1)(x-3)} - \frac{-4x-2}{2(x-1)(x-3)}$$
Multiply.
$$= \frac{x^2-x-6-(-4x-2)}{2(x-1)(x-3)}$$
Subtract numerators.
$$= \frac{x^2+3x-4}{2(x-1)(x-3)}$$
Simplify numerator.
$$= \frac{(x-1)(x+4)}{2(x-1)(x-3)}$$
Factor numerator.
$$= \frac{x+4}{2(x-3)}$$
Simplify.

AVOID ERRORS

After you simplify the numerator, check to see if the numerator has a factor in common with the denominator. If so, the expression can be simplified further.

GUIDED PRACTICE for Examples 2, 3, and 4

Find the least common multiple of the polynomials.

5. $5x^3$ and $10x^2 - 15x$ **6.** $8x - 6x^3 - 15x^2 - 15x^2$

6. 8x - 16 and $12x^2 + 12x - 72$

Perform the indicated operation and simplify.

7.
$$\frac{3}{4x} - \frac{1}{7}$$

8. $\frac{1}{3x^2} + \frac{x}{9x^2 - 12x}$
9. $\frac{x}{x^2 - x - 12} + \frac{5}{12x - 48}$
10. $\frac{x + 1}{x^2 + 4x + 4} - \frac{6}{x^2 - 4}$

KEY CONCEPT

For Your Notebook

Simplifying Complex Fractions

A **complex fraction** is a fraction that contains a fraction in its numerator or denominator. A complex fraction can be simplified using either of the methods below.

Method 1: If necessary, simplify the numerator and denominator by writing each as a single fraction. Then divide the numerator by the denominator.

Method 2: Multiply the numerator and the denominator by the least common denominator (LCD) of *every* fraction in the numerator and denominator. Then simplify.