TRANSFORMING POWER DATA A set of more than two points $(x, y)$ fits a power pattern if and only if the set of transformed points $(\ln x, \ln y)$ fits a linear pattern.

Graph of points ( $x, y$ )


The graph is a power curve.

Graph of points $(\ln x, \ln y)$


The graph is a line.

## EXAMPLE 5 Find a power model

BIOLOGY The table at the right shows the typical wingspans $x$ (in feet) and the typical weights $y$ (in pounds) for several types of birds.

- Draw a scatter plot of the data pairs $(\ln x, \ln y)$. Is a power model a good fit for the original data pairs $(x, y)$ ?
- Find a power model for the original data.

| Bird | Wingspan (ft), $\boldsymbol{x}$ | Weight (lb), $\boldsymbol{y}$ |
| :--- | :---: | :---: |
| Cuckoo | 1.90 | 0.23 |
| Crow | 2.92 | 1.04 |
| Curlew | 3.41 | 1.69 |
| Goose | 5.35 | 6.76 |
| Vulture | 8.40 | 16.03 |
|  |  |  |

## Solution

STEP 1 Use a calculator to create a table of data pairs $(\ln x, \ln y)$.

| $\ln x$ | 0.642 | 1.072 | 1.227 | 1.677 | 2.128 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\ln y$ | -1.470 | 0.039 | 0.525 | 1.911 | 2.774 |

STEP 2 Plot the new points as shown. The points lie close to a line, so a power model should be a good fit for the original data.

STEP 3 Find a power model $y=a x^{b}$ by choosing two points on the line, such as ( $1.227,0.525$ ) and ( $2.128,2.774$ ). Use these points to write an equation of the line. Then solve for $y$.

$\ln y-y_{1}=m\left(\ln x-x_{1}\right)$
$\ln y-2.774=2.5(\ln x-2.128)$

$$
\begin{aligned}
\ln y & =2.5 \ln x-2.546 \\
\ln y & =\ln x^{2.5}-2.546 \\
y & =e^{\ln x^{2.5}-2.546} \\
y & =e^{-2.546} \cdot e^{\ln x^{2.5}} \\
y & =0.0784 x^{2.5}
\end{aligned}
$$

Equation when axes are $\ln x$ and $\ln y$
Substitute.
Simplify.
Power property of logarithms
Exponentiate each side using base $e$.
Product of powers property
Simplify.

