

14. **★ OPENS UP DOWN** Write a function  $f$  such that the graph of  $f^{-1}$  is a line with a slope of 3.

**EXAMPLE 2**

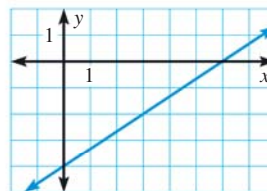
on p. 439  
for Exs. 15–21

**VERIFYING INVERSE FUNCTIONS** Verify that  $f$  and  $g$  are inverse functions.

15.  $f(x) = x + 4, g(x) = x - 4$       16.  $f(x) = 2x + 3, g(x) = \frac{1}{2}x - \frac{3}{2}$   
 17.  $f(x) = \frac{1}{4}x^3, g(x) = (4x)^{1/3}$       18.  $f(x) = \frac{1}{5}x - 1, g(x) = 5x + 5$   
 19.  $f(x) = 4x + 9, g(x) = \frac{1}{4}x - \frac{9}{4}$       20.  $f(x) = 5x^2 - 2, x \geq 0; g(x) = \left(\frac{x+2}{5}\right)^{1/2}$

21. **★ MAKES REASONING** What is the inverse of the function whose graph is shown?

- (A)  $g(x) = \frac{3}{2}x - 6$       (B)  $g(x) = \frac{3}{2}x + 6$   
 (C)  $g(x) = \frac{2}{3}x - 6$       (D)  $g(x) = \frac{3}{2}x + 12$



**EXAMPLE 4**

on p. 440  
for Exs. 22–28

**INVERSES OF POWER FUNCTIONS** Find the inverse of the power function.

22.  $f(x) = x^7$       23.  $f(x) = 4x^4, x \geq 0$       24.  $f(x) = -10x^6, x \leq 0$   
 25.  $f(x) = 32x^5$       26.  $f(x) = -\frac{2}{5}x^3$       27.  $f(x) = \frac{16}{25}x^2, x \leq 0$   
 28. **★ MAKES REASONING** What is the inverse of  $f(x) = -\frac{1}{64}x^3$ ?

- (A)  $g(x) = -4x^3$       (B)  $g(x) = 4\sqrt[3]{x}$       (C)  $g(x) = -4\sqrt[3]{x}$       (D)  $g(x) = \sqrt[3]{-4x}$

**EXAMPLE 5**

on p. 441  
for Exs. 29–43

**HORIZONTAL LINE TEST** Graph the function  $f$ . Then use the graph to determine whether the inverse of  $f$  is a function.

29.  $f(x) = 3x + 1$       30.  $f(x) = -x - 5$       31.  $f(x) = \frac{1}{4}x^2 - 1$   
 32.  $f(x) = -6x^2, x \geq 0$       33.  $f(x) = \frac{1}{3}x^3$       34.  $f(x) = x^3 - 2$   
 35.  $f(x) = (x - 4)(x + 1)$       36.  $f(x) = |x| + 4$       37.  $f(x) = 4x^4 - 5x^2 - 6$

**INVERSES OF NONLINEAR FUNCTIONS** Find the inverse of the function.

38.  $f(x) = \frac{3}{2}x^4, x \geq 0$       39.  $f(x) = x^3 - 2$       40.  $f(x) = \frac{3}{4}x^5 + 5$   
 41.  $f(x) = -\frac{2}{5}x^6 + 8, x \leq 0$       42.  $f(x) = \frac{2x^3 - 6}{9}$       43.  $f(x) = x^4 - 9, x \geq 0$

44. **REASONING** Determine whether the statement is *true* or *false*. Explain your reasoning.  
 a. If  $f(x) = x^n$  where  $n$  is a positive even integer, then the inverse of  $f$  is a function.  
 b. If  $f(x) = x^n$  where  $n$  is a positive odd integer, then the inverse of  $f$  is a function.  
 45. **CHALLENGE** Show that the inverse of any linear function  $f(x) = mx + b$ , where  $m \neq 0$ , is also a linear function. Give the slope and  $y$ -intercept of the graph of  $f^{-1}$  in terms of  $m$  and  $b$ .