

CHAPTER SUMMARY

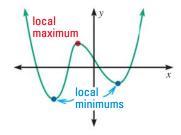
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BIG IDEAS



Graphing Polynomial Functions



The end behavior of the graph of f(x) is

 $f(x) \to +\infty$ as $x \to -\infty$ and $f(x) \to +\infty$ as $x \to +\infty$

so f(x) is of even degree and has a positive leading coefficient.

The graph has 3 turning points, so the degree of f(x) is *at least* 4 and f(x) has *at least* 4 zeros.



Performing Operations with Polynomials

You can add, subtract, multiply, and divide polynomials. You can also factor polynomials using any combination of the methods below.

Factoring method	Example
General trinomial	$6x^2 - 7x - 3 = (3x + 1)(2x - 3)$
Perfect square trinomial	$x^2 + 10x + 25 = (x + 5)^2$
Difference of two squares	$x^2 - 49 = (x + 7)(x - 7)$
Common monomial factor	$15x^3 + 9x^2 = 3x^2(5x + 3)$
Sum or difference of two cubes	$8x^3 - 27 = (2x - 3)(4x^2 + 6x + 9)$
Factor by grouping	$x^{3} - 5x^{2} + 9x - 45 = x^{2}(x - 5) + 9(x - 5) = (x^{2} + 9)(x - 5)$



Solving Polynomial Equations and Finding Zeros

The terms *zero*, *factor*, *solution*, and *x*-*intercept* are closely related. Consider the function $f(x) = 2x^3 - x^2 - 13x - 6$.

−2 is a zero of <i>f</i> .	$f(-2) = 2(-2)^3 - (-2)^2 - 13(-2) - 6 = 0$
x + 2 is a factor of $f(x)$.	$2x^3 - x^2 - 13x - 6 = (x + 2)(x - 3)(2x + 1)$
x = -2 is a solution of the equation $f(x) = 0$.	$2(-2)^3 - (-2)^2 - 13(-2) - 6 = 0$
-2 is an <i>x</i> -intercept of the graph of <i>f</i> .	