22. Worbng bitedimath Write two different cubic functions whose graphs pass through the points $(-3,0),(-1,0)$, and $(2,6)$.
23. Thorstrmereonse How many points do you need to determine a quartic function? a quintic (fifth-degree) function? Justify your answers.
24. Challenge Substitute the expressions $k, k+1, k+2, \ldots, k+5$ for $x$ in the function $f(x)=a x^{3}+b x^{2}+c x+d$ to generate six equally-spaced ordered pairs. Then show that third-order differences are constant.

## PROBLEM SOLVING

EXAMPLE 3
on p. 395
for Ex. 25

EXAMPLE 4
on p. 396
for Exs. 26-28
25. GEOMETRY Find a polynomial function that gives the number of diagonals $d$ of a polygon with $n$ sides.

| Number of sides, $\boldsymbol{n}$ | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of diagonals, $\boldsymbol{d}$ | 0 | 2 | 5 | 9 | 14 | 20 |


26. AVIATION The table shows the number of active pilots (in thousands) with airline transport licenses in the United States for the years 1997 to 2004. Use a graphing calculator to find a polynomial model for the data.

| Years since 1997, $\boldsymbol{t}$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Transport pilots, $\boldsymbol{p}$ | 131 | 135 | 138 | 142 | 145 | 145 | 144 | 145 |

TEXAS @Homeduptublerfosqikoibyehequlaticgabzezprat cdarszone.com
27. MULTI-STEP PROBLEM The table shows the average U.S. movie ticket price (in dollars) for various years from 1983 to 2003.

| Years since 1983, $\boldsymbol{t}$ | 0 | 4 | 8 | 12 | 16 | 20 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Movie ticket price, $\boldsymbol{m}$ | 3.15 | 3.91 | 4.21 | 4.35 | 5.08 | 6.03 |

a. Use a graphing calculator to find a polynomial model for the data.
b. Estimate the average U.S. movie ticket price in 2010.
c. In which year was the average U.S. movie ticket price about $\$ 4.50$ ?
28. Sindrabironse Based on data collected from friends, you estimate the cumulative profits (in dollars) after each of six months for two potential businesses. Find a polynomial function that models the profit for each business. Which business will yield the greatest long-term profit? Why?

| Yard <br> work | Month, $t$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Profit, $p$ | 30 | 210 | 410 | 680 | 1070 | 1630 |
| Pet <br> care | Month, $t$ | 1 | 2 | 3 | 4 | 5 | 6 |
|  | Profit, $p$ | 30 | 50 | 220 | 540 | 1010 | 1630 |

