

23. **★MAKE REASONING** According to the rational zero theorem, which is *not* a possible zero of the function  $f(x) = 2x^4 - 5x^3 + 10x^2 - 9$ ?

(A)  $-9$                       (B)  $-\frac{1}{2}$                       (C)  $\frac{5}{2}$                       (D)  $3$

**FINDING REAL ZEROS** Find all real zeros of the function.

24.  $f(x) = 2x^3 + 2x^2 - 8x - 8$                       25.  $g(x) = 2x^3 - 7x^2 + 9$   
 26.  $h(x) = 2x^3 - 3x^2 - 14x + 15$                       27.  $f(x) = 3x^3 + 4x^2 - 35x - 12$   
 28.  $f(x) = 3x^3 + 19x^2 + 4x - 12$                       29.  $g(x) = 2x^3 + 5x^2 - 11x - 14$   
 30.  $g(x) = 2x^4 + 9x^3 + 5x^2 + 3x - 4$                       31.  $h(x) = 2x^4 - x^3 - 7x^2 + 4x - 4$   
 32.  $h(x) = 3x^4 - 6x^3 - 32x^2 + 35x - 12$                       33.  $f(x) = 2x^4 - 9x^3 + 37x - 30$   
 34.  $f(x) = x^5 - 3x^4 - 5x^3 + 15x^2 + 4x - 12$                       35.  $h(x) = 2x^5 + 5x^4 - 3x^3 - 2x^2 - 5x + 3$

**ERROR ANALYSIS** Describe and correct the error in listing the possible rational zeros of the function.

36.  $f(x) = x^3 + 7x^2 + 2x + 14$   
 Possible zeros:  $1, 2, 7, 14$

37.  $f(x) = 6x^3 - 3x^2 + 12x + 5$   
 Possible zeros:  $\pm 1, \pm 2, \pm 3, \pm 6, \pm \frac{1}{5}, \pm \frac{2}{5}, \pm \frac{3}{5}, \pm \frac{6}{5}$

38. **★OPEN-ENDED** Write a polynomial function  $f$  that has a leading coefficient of 4 and has 12 possible rational zeros according to the rational zero theorem.

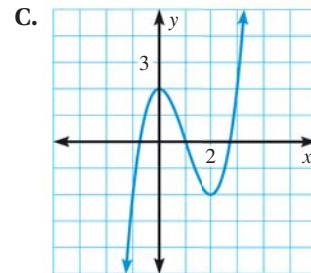
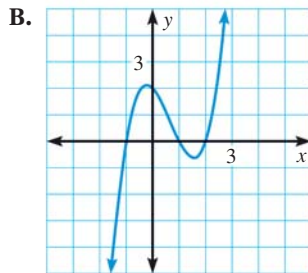
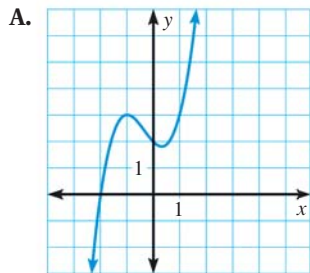
39. **★MAKE REASONING** Which of the following is *not* a zero of the function  $f(x) = 40x^5 - 42x^4 - 107x^3 + 107x^2 + 33x - 36$ ?

(A)  $-\frac{3}{2}$                       (B)  $-\frac{3}{8}$                       (C)  $\frac{3}{4}$                       (D)  $\frac{4}{5}$

40. **★SHORT RESPONSE** Let  $a_n$  be the leading coefficient of a polynomial function  $f$  and  $a_0$  be the constant term. If  $a_n$  has  $r$  factors and  $a_0$  has  $s$  factors, what is the largest number of possible rational zeros of  $f$  that can be generated by the rational zero theorem? *Explain* your reasoning.

**MATCHING** Find all real zeros of the function. Then match each function with its graph.

41.  $f(x) = x^3 - 2x^2 - x + 2$                       42.  $g(x) = x^3 - 3x^2 + 2$                       43.  $h(x) = x^3 + x^2 - x + 2$



44. **CHALLENGE** Is it possible for a cubic function to have more than three real zeros? Is it possible for a cubic function to have no real zeros? *Explain*.