

**EXAMPLE 2**

on p. 354  
for Exs. 10–17

**SUM OR DIFFERENCE OF CUBES** Factor the polynomial completely.

- |                    |                  |                  |                    |
|--------------------|------------------|------------------|--------------------|
| 10. $x^3 + 8$      | 11. $y^3 - 64$   | 12. $27m^3 + 1$  | 13. $125n^3 + 216$ |
| 14. $27a^3 - 1000$ | 15. $8c^3 + 343$ | 16. $192w^3 - 3$ | 17. $-5z^3 + 320$  |

**EXAMPLE 3**

on p. 354  
for Exs. 18–23

**FACTORING BY GROUPING** Factor the polynomial completely.

- |                           |                              |                             |
|---------------------------|------------------------------|-----------------------------|
| 18. $x^3 + x^2 + x + 1$   | 19. $y^3 - 7y^2 + 4y - 28$   | 20. $n^3 + 5n^2 - 9n - 45$  |
| 21. $3m^3 - m^2 + 9m - 3$ | 22. $25s^3 - 100s^2 - s + 4$ | 23. $4c^3 + 8c^2 - 9c - 18$ |

**EXAMPLE 4**

on p. 355  
for Exs. 24–29

**QUADRATIC FORM** Factor the polynomial completely.

- |                  |                           |                            |
|------------------|---------------------------|----------------------------|
| 24. $x^4 - 25$   | 25. $a^4 + 7a^2 + 6$      | 26. $3s^4 - s^2 - 24$      |
| 27. $32z^5 - 2z$ | 28. $36m^6 + 12m^4 + m^2$ | 29. $15x^5 - 72x^3 - 108x$ |

**EXAMPLE 5**

on p. 355  
for Exs. 30–41

**ERROR ANALYSIS** Describe and correct the error in finding all real-number solutions.

30.

$$\begin{aligned} 8x^3 - 27 &= 0 \\ (2x + 3)(4x^2 + 6x + 9) &= 0 \\ x = -\frac{3}{2} \end{aligned}$$

31.

$$\begin{aligned} 3x^3 - 48x &= 0 \\ 3x(x^2 - 16) &= 0 \\ x^2 - 16 &= 0 \\ x = -4 \text{ or } x = 4 \end{aligned}$$

**SOLVING EQUATIONS** Find the real-number solutions of the equation.

- |                                |                                  |                              |
|--------------------------------|----------------------------------|------------------------------|
| 32. $y^3 - 5y^2 = 0$           | 33. $18s^3 = 50s$                | 34. $g^3 + 3g^2 - g - 3 = 0$ |
| 35. $m^3 + 6m^2 - 4m - 24 = 0$ | 36. $4w^4 + 40w^2 - 44 = 0$      | 37. $4z^5 = 84z^3$           |
| 38. $5b^3 + 15b^2 + 12b = -36$ | 39. $x^6 - 4x^4 - 9x^2 + 36 = 0$ | 40. $48p^5 = 27p^3$          |

41.  **TAKS REASONING** What are the real-number solutions of the equation  $3x^4 - 27x^2 + 9x = x^3$ ?

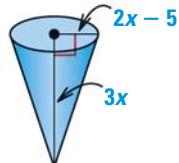
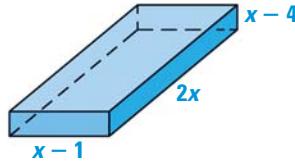
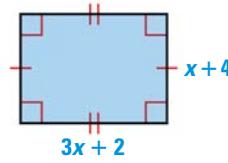
- (A)  $-1, 0, 3$       (B)  $-3, 0, 3$       (C)  $-3, 0, \frac{1}{3}, 3$       (D)  $-3, -\frac{1}{3}, 0, 3$

**CHOOSING A METHOD** Factor the polynomial completely using any method.

- |                                |                             |                             |
|--------------------------------|-----------------------------|-----------------------------|
| 42. $16x^3 - 44x^2 - 42x$      | 43. $n^4 - 4n^2 - 60$       | 44. $-4b^4 - 500b$          |
| 45. $36a^3 - 15a^2 + 84a - 35$ | 46. $18c^4 + 57c^3 - 10c^2$ | 47. $2d^4 - 13d^2 - 45$     |
| 48. $32x^5 - 108x^2$           | 49. $8y^6 - 38y^4 - 10y^2$  | 50. $z^5 - 3z^4 - 16z + 48$ |

 **GEOMETRY** Find the possible value(s) of  $x$ .

51. Area = 48      52. Volume = 40      53. Volume =  $125\pi$

**CHOOSING A METHOD** Factor the polynomial completely using any method.

- |   |                                   |                         |
|---|-----------------------------------|-------------------------|
| 54. $x^3y^6 - 27$   | 55. $7ac^2 + bc^2 - 7ad^2 - bd^2$ | 56. $x^{2n} - 2x^n + 1$ |
| 57. <b>CHALLENGE</b> Factor $a^5b^2 - a^2b^4 + 2a^4b - 2ab^3 + a^3 - b^2$ completely. |                                   |                         |