SCIENTIFIC NOTATION A number is expressed in scientific notation if it is in the form $c \times 10^n$ where $1 \le c < 10$ and n is an integer. When you work with numbers in scientific notation, the properties of exponents can make calculations easier.

EXAMPLE 2

Use scientific notation in real life

LOCUSTS A swarm of locusts may contain as many as 85 million locusts per square kilometer and cover an area of 1200 square kilometers. About how many locusts are in such a swarm?

Solution

Number of locusts

Number of square kilometers



$$= 85,000,000 \times 1200$$

Substitute values.

$$= (8.5 \times 10^7)(1.2 \times 10^3)$$

Write in scientific notation.

$$= (8.5 \times 1.2) (10^7 \times 10^3)$$

Use multiplication properties.

$$= 10.2 \times 10^{10}$$

Product of powers property

$$= 1.02 \times 10^1 \times 10^{10}$$

Write 10.2 in scientific notation.

$$= 1.02 \times 10^{11}$$

Product of powers property

The number of locusts is about 1.02×10^{11} , or about 102,000,000,000.



GUIDED PRACTICE for Examples 1 and 2

Evaluate the expression. Tell which properties of exponents you used.

1.
$$(4^2)^3$$

3.
$$\left(\frac{2}{9}\right)^3$$

2.
$$(-8)(-8)^3$$
 3. $\left(\frac{2}{9}\right)^3$ **4.** $\frac{6 \cdot 10^{-4}}{9 \cdot 10^7}$

SIMPLIFYING EXPRESSIONS You can use the properties of exponents to simplify algebraic expressions. A simplified expression contains only positive exponents.

EXAMPLE 3 Simplify expressions

a.
$$b^{-4}b^{6}b^{7} = b^{-4+6+7} = b^{9}$$
 Product of powers property

NOTATION

For help with scientific

notation, see p. 982.

In this book, it is assumed that any base with a zero or negative exponent is nonzero.

b.
$$\left(\frac{r^{-2}}{s^3}\right)^{-3} = \frac{(r^{-2})^{-3}}{(s^3)^{-3}}$$
 Power of a quotient property

$$=\frac{r^6}{s^{-9}}$$

 $= \frac{r^6}{s^{-9}}$ Power of a power property

$$= r^6 s^9$$

Negative exponent property

c.
$$\frac{16m^4n^{-5}}{2n^{-5}} = 8m^4n^{-5-(-5)}$$
 Quotient of powers property

$$=8m^4n^0=8m^4$$

 $=8m^4n^0=8m^4$ **Zero exponent property**

Animated Algebra at classzone.com