**GEOMETRY** Solve the formula for the variable in red. Then use the given information to find the value of the variable. Round to the nearest tenth.

18. Area of a circular ring

$$A = 2\pi rw$$



Find r if w = 4 ft and A = 120 ft<sup>2</sup>.

19. Lateral surface area of a truncated cylinder

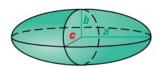
$$S = \pi r(\mathbf{h} + k)$$



Find h if r = 2 cm, k = 3 cm, and S = 50 cm<sup>2</sup>.

## 20. Volume of an ellipsoid

$$V = \frac{4}{3}\pi ab\mathbf{c}$$



Find *c* if a = 4 in., b = 3 in., and V = 60 in.<sup>3</sup>

## **EXAMPLE 4**

on p. 28 for Exs. 21–26 **REWRITING EQUATIONS** Solve the equation for y. Then find the value of y for the given value of x.

**21.** 
$$xy - 3x = 40$$
;  $x = 5$ 

**23.** 
$$3xy - 28 = 16x$$
;  $x = 4$ 

**25.** 
$$y - 2xy = 15$$
;  $x = -1$ 

**22.** 
$$7x - xy = -18$$
;  $x = -4$ 

**24.** 
$$9y + 6xy = 30$$
;  $x = -6$ 

**26.** 
$$4x + 7y + 5xy = 0$$
;  $x = 1$ 

- **27. TO FINE ASPORNSE** Consider the equation 15x 9y = 27. To find the value of y when x = 2, you can use two methods.
  - **Method 1** *Solve the original equation for y and then substitute 2 for x.*
  - **Method 2** *Substitute 2 for x and then solve the resulting equation for y.*

Show the steps of the two methods. Which method is more efficient if you need to find the value of *y* for several values of *x*? *Explain*.

**REASONING** Solve for the indicated variable.

**28.** Solve 
$$xy = x + y$$
 for  $y$ .

**29.** Solve 
$$xyz = x + y + z$$
 for *z*.

**30.** Solve 
$$\frac{1}{x} + \frac{1}{y} = 1$$
 for *y*.

**31.** Solve 
$$\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 1$$
 for z.

**32. CHALLENGE** Write a formula giving the area of a circle in terms of its circumference.

## PROBLEM SOLVING

## **EXAMPLE 5**

on p. 29 for Exs. 33–38 **33. TREE DIAMETER** You can estimate the diameter of a tree without boring through it by measuring its circumference. Solve the formula  $C = \pi d$  for d. Then find the diameter of an oak that has a circumference of 113 inches.

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**34. DESIGN** The fabric panels on a kite are rhombuses. A formula for the length of the long diagonal d is  $d = s\sqrt{3}$  where s is the length of a side. Solve the formula for s. Then find the value of s when d = 15 inches.

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