SYSTEMS OF THREE OR MORE INEQUALITIES You can also graph a system of three or more linear inequalities, as shown in Example 4.



EXAMPLE 4) TAKS REASONING: Multi-Step Problem

SHOPPING A discount shoe store is having a sale, as described in the advertisement shown.

- Use the information in the ad to write a system of inequalities for the regular footwear prices and possible sale prices.
- Graph the system of inequalities.
- Use the graph to estimate the range of possible sale prices for footwear that is regularly priced at \$70.



80

60

40

20

٥

0

20

Sale price (dollars)

x = 80

x = 20

= 0.9x

40 60

Regular price (dollars)

0 4

80 X

Solution

- *STEP 1* Write a system of inequalities. Let *x* be the regular footwear price and let *y* be the sale price. From the information in the ad, you can write the following four inequalities.
 - $x \ge 20$ Regular price must be at least \$20.
 - $x \le 80$ Regular price can be at most \$80.
 - $y \ge 0.4x$ Sale price is at least (100 60)% = 40% of regular price.
 - $y \le 0.9x$ Sale price is at most (100 10)% = 90% of regular price.
- *STEP 2* **Graph** each inequality in the system. Then identify the region that is common to all the graphs. It is the region that is shaded.
- *STEP 3* Identify the range of possible sale prices for \$70 footwear. From the graph you can see that when x = 70, the value of y is between these values:

0.4(70) = 28 and 0.9(70) = 63

So, the value of *y* satisfies $28 \le y \le 63$.

Therefore, footwear regularly priced at \$70 sells for between \$28 and \$63, inclusive, during the sale.

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GUIDED PRACTICE for Example 4

- **7. WHAT IF?** In Example 4, suppose the advertisement showed a range of discounts of 20%–50% and a range of regular prices of \$40–\$100.
 - **a.** Write and graph a system of inequalities for the regular footwear prices and possible sale prices.
 - **b.** Use the graph to estimate the range of possible sale prices for footwear that is regularly priced at \$60.