

Graphing a Linear Inequality

To graph a linear inequality in two variables, follow these steps:

STEP 1 **Graph** the boundary line for the inequality. Use a dashed line for $<$ or $>$ and a solid line for \leq or \geq .

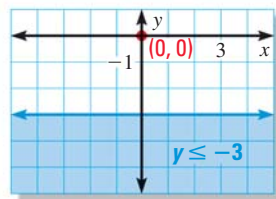
STEP 2 **Test** a point *not* on the boundary line to determine whether it is a solution of the inequality. If it is a solution, shade the half-plane containing the point. If it is not a solution, shade the other half-plane.

EXAMPLE 2 Graph linear inequalities with one variable

Graph (a) $y \leq -3$ and (b) $x < 2$ in a coordinate plane.

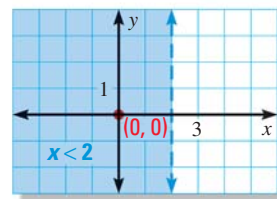
a. **Graph** the boundary line $y = -3$. Use a solid line because the inequality symbol is \leq .

Test the point $(0, 0)$. Because $(0, 0)$ is *not* a solution of the inequality, shade the half-plane that does not contain $(0, 0)$.



b. **Graph** the boundary line $x = 2$. Use a dashed line because the inequality symbol is $<$.

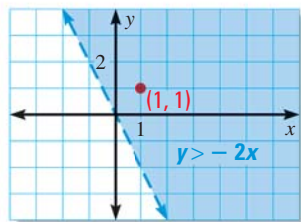
Test the point $(0, 0)$. Because $(0, 0)$ is a solution of the inequality, shade the half-plane that contains $(0, 0)$.

**EXAMPLE 3** Graph linear inequalities with two variables

Graph (a) $y > -2x$ and (b) $5x - 2y \leq -4$ in a coordinate plane.

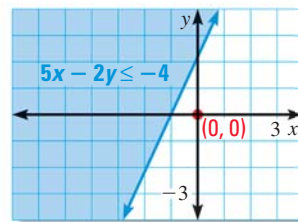
a. **Graph** the boundary line $y = -2x$. Use a dashed line because the inequality symbol is $>$.

Test the point $(1, 1)$. Because $(1, 1)$ is a solution of the inequality, shade the half-plane that contains $(1, 1)$.



b. **Graph** the boundary line $5x - 2y = -4$. Use a solid line because the inequality symbol is \leq .

Test the point $(0, 0)$. Because $(0, 0)$ is *not* a solution of the inequality, shade the half-plane that does not contain $(0, 0)$.

**AVOID ERRORS**

It is often convenient to use $(0, 0)$ as a test point. However, if $(0, 0)$ lies on the boundary line, you must choose a different test point.