

Formulas and Identities from Trigonometry (continued)

Law of cosines (p. 889)	<p>If $\triangle ABC$ has sides of length a, b, and c, then:</p> $a^2 = b^2 + c^2 - 2bc \cos A$ $b^2 = a^2 + c^2 - 2ac \cos B$ $c^2 = a^2 + b^2 - 2ab \cos C$
Heron's area formula (p. 891)	<p>The area of the triangle with sides of length a, b, and c is</p> $\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$ <p>where $s = \frac{1}{2}(a + b + c)$.</p>
Reciprocal identities (p. 924)	$\csc \theta = \frac{1}{\sin \theta} \qquad \sec \theta = \frac{1}{\cos \theta} \qquad \cot \theta = \frac{1}{\tan \theta}$
Tangent and cotangent identities (p. 924)	$\tan \theta = \frac{\sin \theta}{\cos \theta} \qquad \cot \theta = \frac{\cos \theta}{\sin \theta}$
Pythagorean identities (p. 924)	$\sin^2 \theta + \cos^2 \theta = 1 \qquad 1 + \tan^2 \theta = \sec^2 \theta \qquad 1 + \cot^2 \theta = \csc^2 \theta$
Cofunction identities (p. 924)	$\sin\left(\frac{\pi}{2} - \theta\right) = \cos \theta \qquad \cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta \qquad \tan\left(\frac{\pi}{2} - \theta\right) = \cot \theta$
Negative angle identities (p. 924)	$\sin(-\theta) = -\sin \theta \qquad \cos(-\theta) = \cos \theta \qquad \tan(-\theta) = -\tan \theta$
Sum formulas (p. 949)	$\sin(a + b) = \sin a \cos b + \cos a \sin b$ $\cos(a + b) = \cos a \cos b - \sin a \sin b$ $\tan(a + b) = \frac{\tan a + \tan b}{1 - \tan a \tan b}$
Difference formulas (p. 949)	$\sin(a - b) = \sin a \cos b - \cos a \sin b$ $\cos(a - b) = \cos a \cos b + \sin a \sin b$ $\tan(a - b) = \frac{\tan a - \tan b}{1 + \tan a \tan b}$
Double-angle formulas (p. 955)	$\cos 2a = \cos^2 a - \sin^2 a \qquad \sin 2a = 2 \sin a \cos a$ $\cos 2a = 2 \cos^2 a - 1 \qquad \tan 2a = \frac{2 \tan a}{1 - \tan^2 a}$ $\cos 2a = 1 - 2 \sin^2 a$
Half-angle formulas (p. 955)	$\sin \frac{a}{2} = \pm \sqrt{\frac{1 - \cos a}{2}} \qquad \tan \frac{a}{2} = \frac{1 - \cos a}{\sin a}$ $\cos \frac{a}{2} = \pm \sqrt{\frac{1 + \cos a}{2}} \qquad \tan \frac{a}{2} = \frac{\sin a}{1 + \cos a}$ <p>The signs of $\sin \frac{a}{2}$ and $\cos \frac{a}{2}$ depend on the quadrant in which $\frac{a}{2}$ lies.</p>