

Formulas for Sequences and Series

Formulas for sums of special series (p. 797)	$\sum_{i=1}^n 1 = n$ $\sum_{i=1}^n i = \frac{n(n+1)}{2}$ $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$
Explicit rule for an arithmetic sequence (p. 802)	<p>The nth term of an arithmetic sequence with first term a_1 and common difference d is:</p> $a_n = a_1 + (n-1)d$
Sum of a finite arithmetic series (p. 804)	<p>The sum of the first n terms of an arithmetic series is:</p> $S_n = n \left(\frac{a_1 + a_n}{2} \right)$
Explicit rule for a geometric sequence (p. 810)	<p>The nth term of a geometric sequence with first term a_1 and common ratio r is:</p> $a_n = a_1 r^{n-1}$
Sum of a finite geometric series (p. 812)	<p>The sum of the first n terms of a geometric series with common ratio $r \neq 1$ is:</p> $S_n = a_1 \left(\frac{1-r^n}{1-r} \right)$
Sum of an infinite geometric series (p. 821)	<p>The sum of an infinite geometric series with first term a_1 and common ratio r is</p> $S = \frac{a_1}{1-r}$ <p>provided $r < 1$. If $r \geq 1$, the series has no sum.</p>
Recursive equation for an arithmetic sequence (p. 827)	$a_n = a_{n-1} + d$ <p>where d is the common difference</p>
Recursive equation for a geometric sequence (p. 827)	$a_n = r \cdot a_{n-1}$ <p>where r is the common ratio</p>

Formulas and Identities from Trigonometry

Conversion between degrees and radians (p. 860)	<p>To rewrite a degree measure in radians, multiply by $\frac{\pi \text{ radians}}{180^\circ}$.</p> <p>To rewrite a radian measure in degrees, multiply by $\frac{180^\circ}{\pi \text{ radians}}$.</p>
Definition of trigonometric functions (p. 866)	<p>Let θ be an angle in standard position and (x, y) be any point (except the origin) on the terminal side of θ. Let $r = \sqrt{x^2 + y^2}$.</p> $\sin \theta = \frac{y}{r} \qquad \cos \theta = \frac{x}{r} \qquad \tan \theta = \frac{y}{x}, x \neq 0$ $\csc \theta = \frac{r}{y}, y \neq 0 \qquad \sec \theta = \frac{r}{x}, x \neq 0 \qquad \cot \theta = \frac{x}{y}, y \neq 0$
Law of sines (p. 882)	<p>If $\triangle ABC$ has sides of length a, b, and c, then:</p> $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$
Area of a triangle (given two sides and the included angle) (p. 885)	<p>If $\triangle ABC$ has sides of length a, b, and c, then its area is:</p> $\text{Area} = \frac{1}{2}bc \sin A \qquad \text{Area} = \frac{1}{2}ac \sin B \qquad \text{Area} = \frac{1}{2}ab \sin C$