## Formulas

## Formulas from Coordinate Geometry

| Slope of a line (p. 82) | $m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$ where $m$ is the slope of the nonvertical line through <br> points $\left(x_{1}, y_{1}\right)$ and $\left(x_{2}, y_{2}\right)$ |
| :--- | :--- |
| Parallel and perpendicular <br> lines (p. 84) | If line $l_{1}$ has slope $m_{1}$ and line $l_{2}$ has slope $m_{2}$, then: <br> $l_{1} \\| l_{2}$ if and only if $m_{1}=m_{2}$ <br> $l_{1} \perp l_{2}$ if and only if $m_{1}=-\frac{1}{m_{2}}$, or $m_{1} m_{2}=-1$ |
| Distance formula (p. 615) | $d=\sqrt{\left(x_{2}-x_{1}\right)^{2}+\left(y_{2}-y_{1}\right)^{2}}$ where $d$ is the distance between <br> points $\left(x_{1}, y_{1}\right)$ and $\left(x_{2}, y_{2}\right)$ |
| Midpoint formula (p. 615) | $M\left(\frac{x_{1}+x_{2}}{2}, \frac{y_{1}+y_{2}}{2}\right)$ is the midpoint of the line segment joining |
| points $\left(x_{1}, y_{1}\right)$ and $\left(x_{2}, y_{2}\right)$. |  |

## Formulas from Matrix Algebra

| Determinant of a $2 \times 2$ matrix (p. 203) | $\operatorname{det}\left[\begin{array}{ll}a & b \\ c & d\end{array}\right]=\left\|\begin{array}{ll}a & b \\ c & d\end{array}\right\|=a d-c b$ |
| :---: | :---: |
| Determinant of a $3 \times 3$ matrix <br> (p. 203) | $\operatorname{det}\left[\begin{array}{lll}a & b & c \\ d & e & f \\ g & h & i\end{array}\right]=\left\|\begin{array}{lll}a & b & c \\ d & e & f \\ g & h & i\end{array}\right\|=(a e i+h f g+c d h)-(g e c+h f a+i d b)$ |
| Area of a triangle (p. 204) | The area of a triangle with vertices $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right)$, and $\left(x_{3}, y_{3}\right)$ is given by $\text { Area }= \pm \frac{1}{2}\left\|\begin{array}{lll} x_{1} & y_{1} & 1 \\ x_{2} & y_{2} & 1 \\ x_{3} & y_{3} & 1 \end{array}\right\|$ <br> where the appropriate sign ( $\pm$ ) should be chosen to yield a positive value. |
| $\begin{aligned} & \text { Cramer's rule } \\ & \text { (p. 205) } \end{aligned}$ | Let $A=\left[\begin{array}{ll}a & b \\ c & d\end{array}\right] \begin{gathered}\text { be the coefficient matrix of this linear system: } \\ a x+b y=e\end{gathered}$ $\begin{aligned} & a x+b y=e \\ & c x+d y=f \end{aligned}$ <br> If $\operatorname{det} A \neq 0$, then the system has exactly one solution. <br> The solution is $x=\frac{\left\|\begin{array}{ll}e & b \\ f & d\end{array}\right\|}{\operatorname{det} A}$ and $y=\frac{\left\|\begin{array}{ll}a & e \\ c & f\end{array}\right\|}{\operatorname{det} A}$. |
| Inverse of a $2 \times 2$ matrix (p. 210) | The inverse of the matrix $A=\left[\begin{array}{ll}a & b \\ c & d\end{array}\right]$ is $A^{-1}=\frac{1}{\|A\|}\left[\begin{array}{rr} d & -b \\ -c & a \end{array}\right]=\frac{1}{a d-c b}\left[\begin{array}{rr} d & -b \\ -c & a \end{array}\right] \text { provided } a d-c b \neq 0 .$ |

