

Chapter 6

6.1 Find the indicated real n th root(s) of a .

1. $n = 4, a = 81$

2. $n = 3, a = 512$

3. $n = 5, a = -243$

6.1 Evaluate the expression without using a calculator.

4. $36^{-1/2}$

5. $64^{5/6}$

6. $(\sqrt[3]{216})^{-2}$

7. $(\sqrt[5]{-32})^4$

6.1 Solve the equation. Round the result to two decimal places when appropriate.

8. $x^3 = -8$

9. $x^4 + 9 = 90$

10. $(x - 3)^5 = 60$

11. $-4x^6 = -400$

6.2 Simplify the expression.

12. $4^{5/2} \cdot 4^{-1/2}$

13. $\frac{17^{3/7}}{17^{4/7}}$

14. $(\sqrt[4]{5} \cdot \sqrt{5})^4$

15. $\frac{\sqrt[3]{135}}{\sqrt[3]{5}}$

16. $5\sqrt[5]{7} - 7\sqrt[5]{7}$

17. $\sqrt[3]{2} + 2\sqrt[3]{128}$

18. $\frac{324^{1/4}}{4^{-1/4}}$

19. $4\sqrt[3]{108} \cdot 2\sqrt[3]{4}$

6.2 Write the expression in simplest form. Assume all variables are positive.

20. $\sqrt{20x^6y^7}$

21. $\sqrt[5]{18x^3y^{14}z^{20}}$

22. $\sqrt[4]{\frac{x^5}{y^{16}}}$

23. $\sqrt[3]{16x^7y^2} \cdot \sqrt[3]{6xy^5}$

6.3 Let $f(x) = -x + 4$, $g(x) = x^3$, and $h(x) = \frac{x}{4}$. Perform the indicated operation and state the domain.

24. $f(x) + g(x)$

25. $g(x) - f(x)$

26. $g(x) \cdot h(x)$

27. $\frac{f(x)}{g(x)}$

28. $f(g(x))$

29. $g(h(x))$

30. $h(f(x))$

31. $f(f(x))$

6.4 Verify that f and g are inverse functions.

32. $f(x) = 2x - 4, g(x) = \frac{1}{2}x + 2$

33. $f(x) = 3x^2 + 1, x \geq 0; g(x) = \left(\frac{x-1}{3}\right)^{1/2}$

6.4 Find the inverse of the function.

34. $f(x) = 5x - 3$

35. $f(x) = \frac{4}{3}x + 2$

36. $f(x) = \frac{1}{2}x^2, x \geq 0$

37. $f(x) = -x^6 + 2, x \leq 0$

38. $f(x) = \frac{4x^4 - 1}{18}, x \geq 0$

39. $f(x) = 32x^5 + 4$

6.5 Graph the function. Then state the domain and range.

40. $y = -\frac{1}{3}\sqrt{x}$

41. $y = \frac{2}{5}\sqrt[3]{x}$

42. $y = \frac{5}{6}\sqrt{x}$

43. $y = \sqrt{x+2} - 3$

44. $y = -2\sqrt[3]{x-1} + 2$

45. $f(x) = 3\sqrt[3]{x}$

46. $g(x) = -\frac{1}{2}\sqrt{x-2}$

47. $h(x) = -\sqrt{x+3} + 4$

6.6 Solve the equation. Check your solution.

48. $\sqrt{2x+3} = 7$

49. $-5\sqrt{x+1} + 12 = 2$

50. $\sqrt[3]{5x-1} + 6 = 10$

51. $2\sqrt[3]{8x} + 9 = 5$

52. $7x^{4/3} = 175$

53. $(x-2)^{3/4} = 1$

54. $x - 8 = \sqrt{18x}$

55. $x = \sqrt{4x-3}$

56. $\sqrt{2x+1} + 5 = \sqrt{x+12} - 8$