

Venn Diagrams TEKS 8.12.C

A **Venn diagram** uses shapes to show how sets are related.

EXAMPLE

Draw a Venn diagram of the positive integers less than 13 where set A consists of factors of 12 and set B consists of even numbers.

Positive integers less than 13:

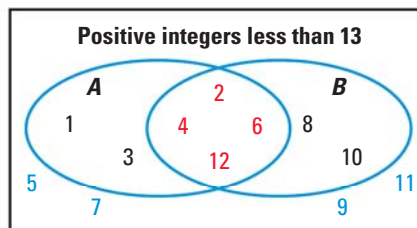
1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12

Set A (factors of 12): 1, 2, 3, 4, 6, 12

Set B (even numbers): 2, 4, 6, 8, 10, 12

Both set A and set B : **2, 4, 6, 12**

Neither set A nor set B : **5, 7, 9, 11**



EXAMPLE

Use the Venn diagram above to decide if the statement is *true* or *false*. Explain your reasoning.

- If a positive integer less than 13 is not even, then it is not a factor of 12.
 - ▶ False. 1 and 3 are not even, but they are factors of 12.
- All positive integers less than 13 that are even are factors of 12.
 - ▶ False. 8 and 10 are even, but they are not factors of 12.

PRACTICE

Draw a Venn diagram of the sets described.

- Of the positive integers less than 11, set A consists of factors of 10 and set B consists of odd numbers.
- Of the positive integers less than 10, set A consists of prime numbers and set B consists of even numbers.
- Of the positive integers less than 25, set A consists of multiples of 3 and set B consists of multiples of 4.

Use the Venn diagrams you drew in Exercises 1–3 to decide if the statement is *true* or *false*. Explain your reasoning.

- The only factors of 10 less than 11 that are not odd are 2 and 10.
- If a number is neither a multiple of 3 nor a multiple of 4, then it is odd.
- All prime numbers less than 10 are not even.
- If a positive odd integer less than 11 is a factor of 10, then it is 5.
- There are 2 positive integers less than 25 that are both a multiple of 3 and a multiple of 4.
- If a positive even integer less than 10 is prime, then it is 2.